

# Kanerva++: extending the Kanerva machine with differentiable, locally block allocated latent memory.

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# Kanerva machine & Dynamic Kanerva machine [3,4]

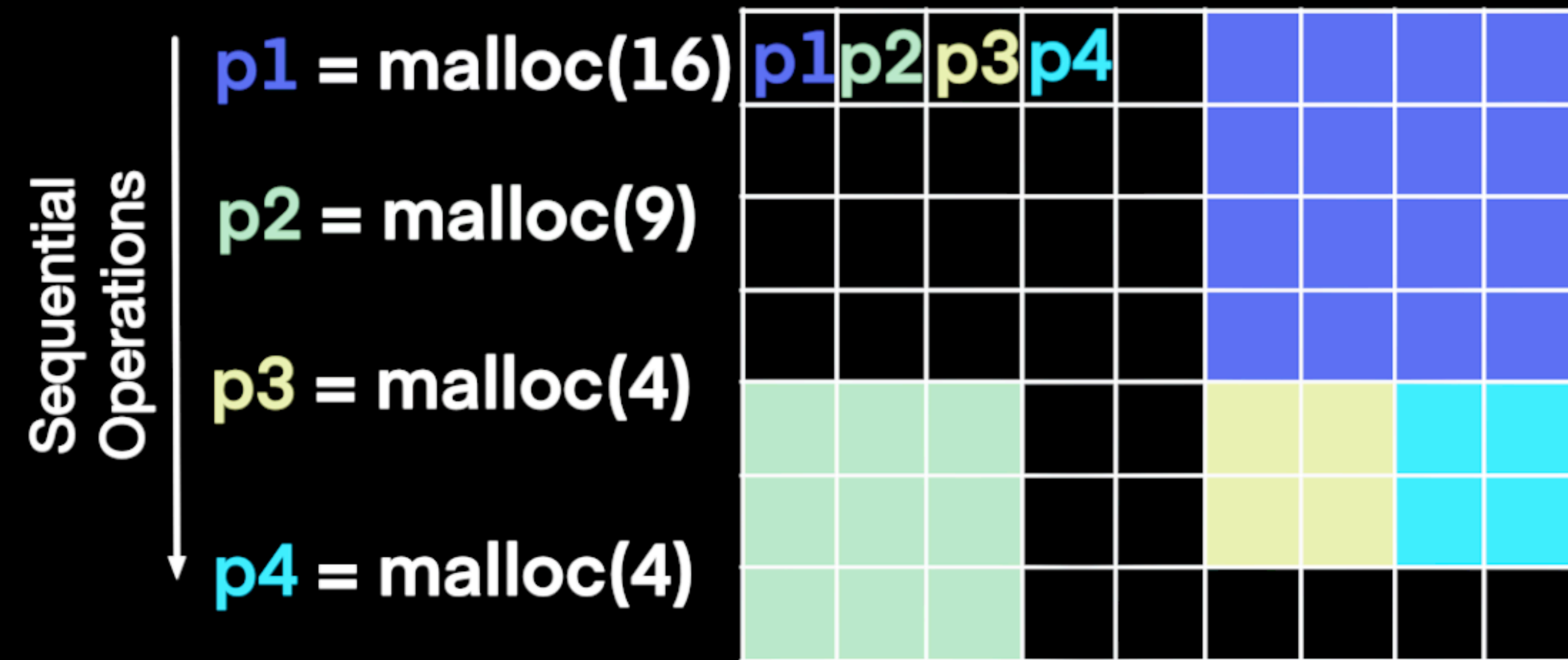
$$M \sim p(M) = \mathcal{N}(U, R, C)$$

- Memory treated as a distribution.
- Writes are inference:  $p(M | X)$
- Reads are sampling conditional:  $p(X | M)$

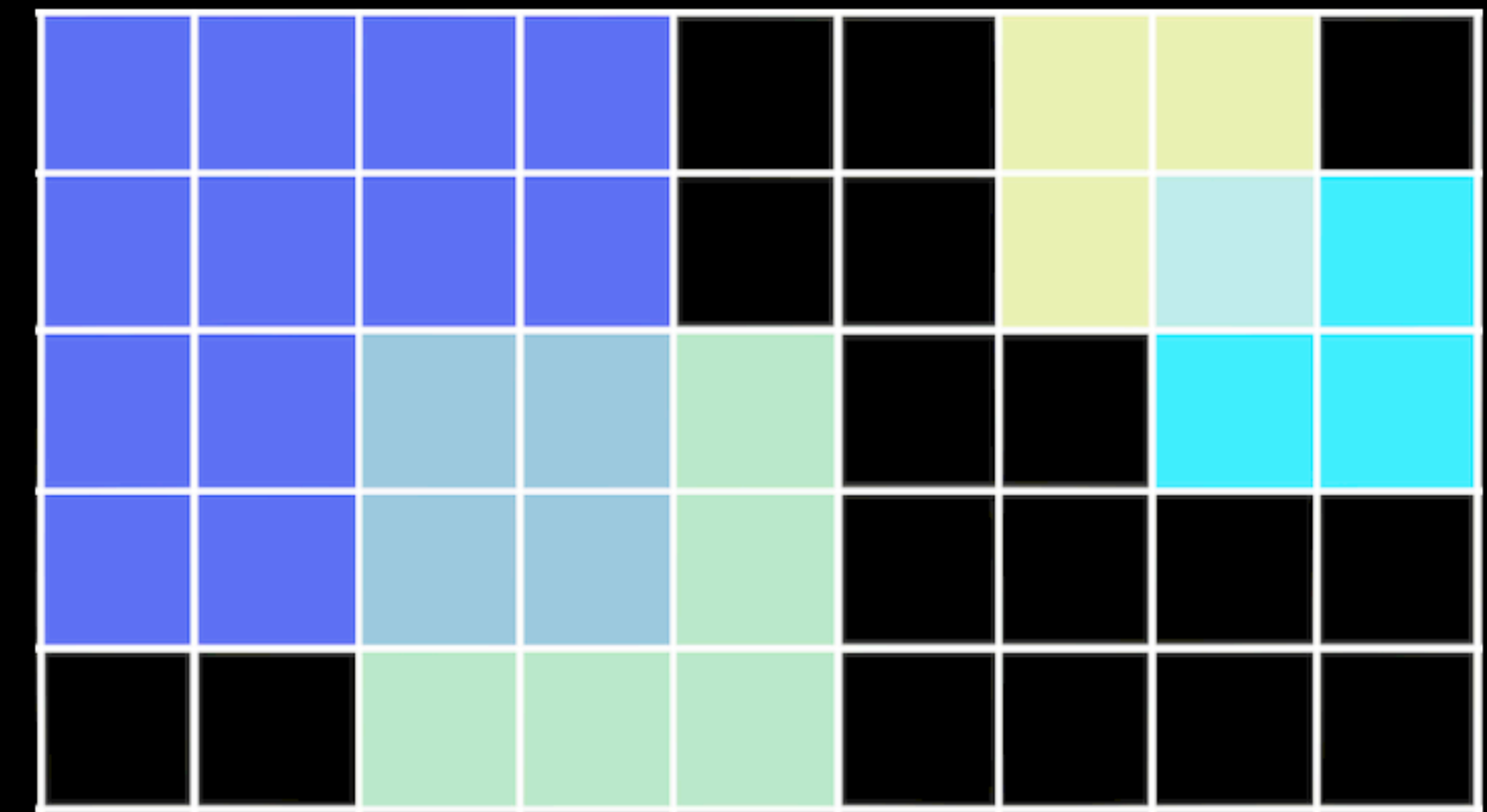
[3] Wu, Yan, et al. "The Kanerva Machine: A Generative Distributed Memory." ICLR. 2018.

[4] Wu, Yan, et al. "Learning attractor dynamics for generative memory." *Advances in Neural Information Processing Systems*. 2018.

# Heap allocator vs. Kanerva++

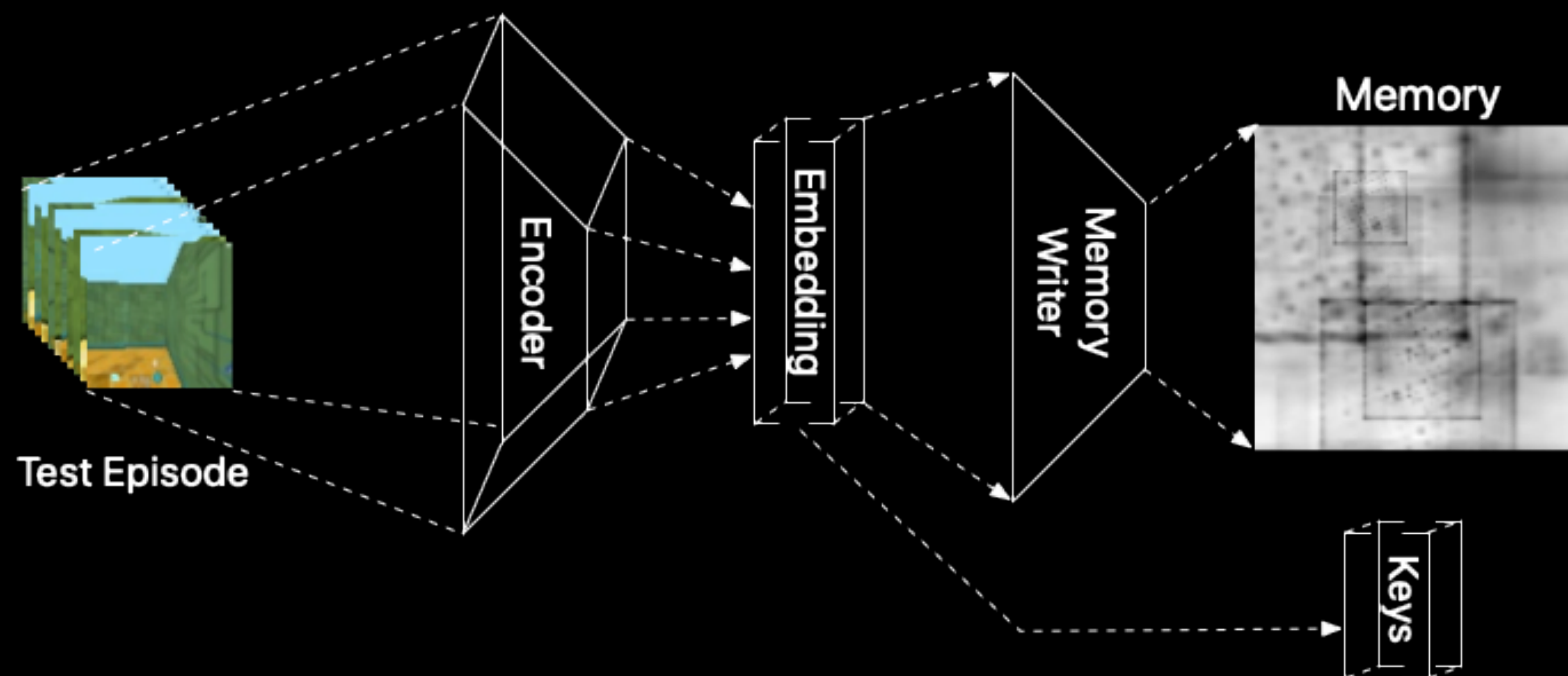


Traditional allocator



K++ allocator

# Write model.



sample episode:

$$X_t = \{x_1, \dots, x_T\} \sim \mathcal{D};$$

compute embedding:

$$E = f_{\theta_{enc}}(X_t);$$

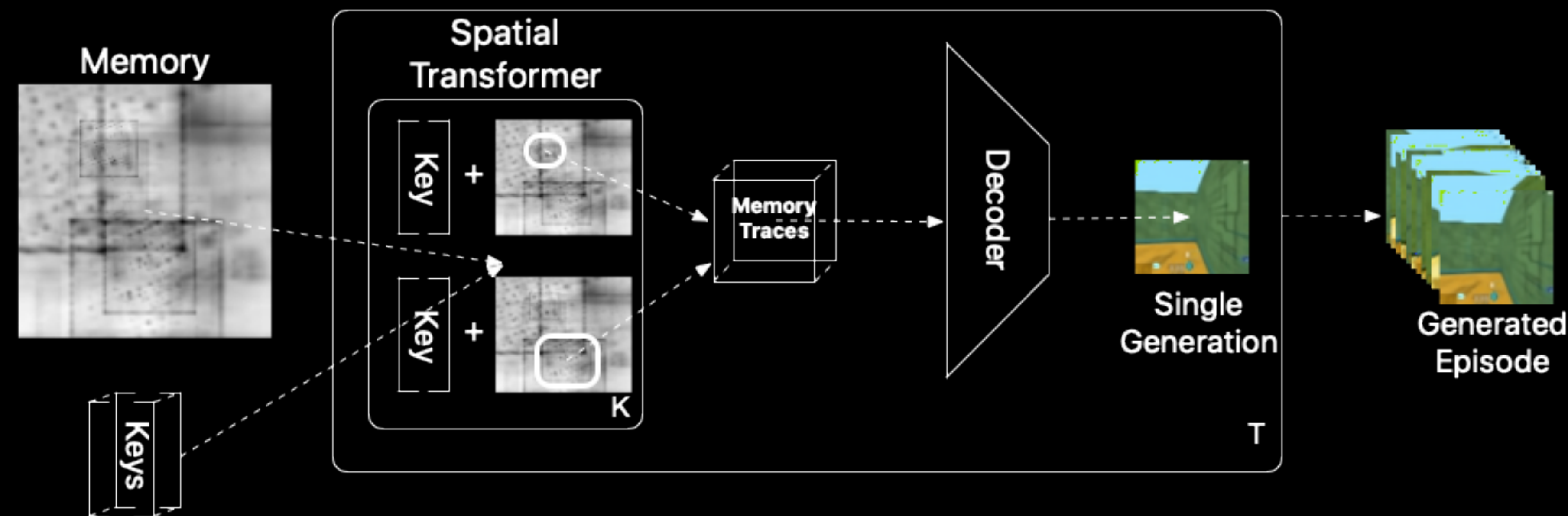
infer keys:  $Y_t \sim$

$$\mathcal{N}(\mu_{\theta_{key}}(E), \sigma_{\theta_{key}}^2(E));$$

write memory:

$$M \sim \delta(f_{\theta_{mem}}(E))$$

# Generative model.



given memory:  $M$  ;  
 sample keys:  $Y_t \sim P(Y_t)$  ;  
 extract regions:  $\hat{M} = \{f_{\theta_{ST}}(M, y_{tk})\}_{k=1}^K$  ;  
 infer latent:  $Z_t \sim \mathcal{N}(\mu_{\theta_Z}(\hat{M}), \sigma_{\theta_Z}^2(\hat{M}))$  ;  
 decode:  $\hat{X}_t \sim \mathcal{N}(\mu_{\theta_{dec}}(\mu_{Z_t}), \sigma^2)$



# Optimization objective.

$$\mathcal{L}_T \approx \mathbb{E}_{q_\phi(Z|X), q_\phi(Y|X)} \ln p_\theta(X|Z, \hat{M}, Y)$$

$$\underbrace{\mathbb{E}_{q_\phi(Y|X)} \mathcal{D}_{KL}[q_\phi(Z|X) || p_\theta(Z|\hat{M}, Y)]}_{\text{Amortized latent variable posterior vs. learned prior}}$$

$$\underbrace{\mathcal{D}_{KL}[q_\phi(Y|X) || p(Y)]}_{\text{Amortized key posterior vs. key prior}}$$

Deterministic memory

$$\hat{M} \sim \delta \left[ \{f_{ST}(M, y_{tk})\}_{k=1}^K \right]$$

# Results: memory conditional likelihood estimation

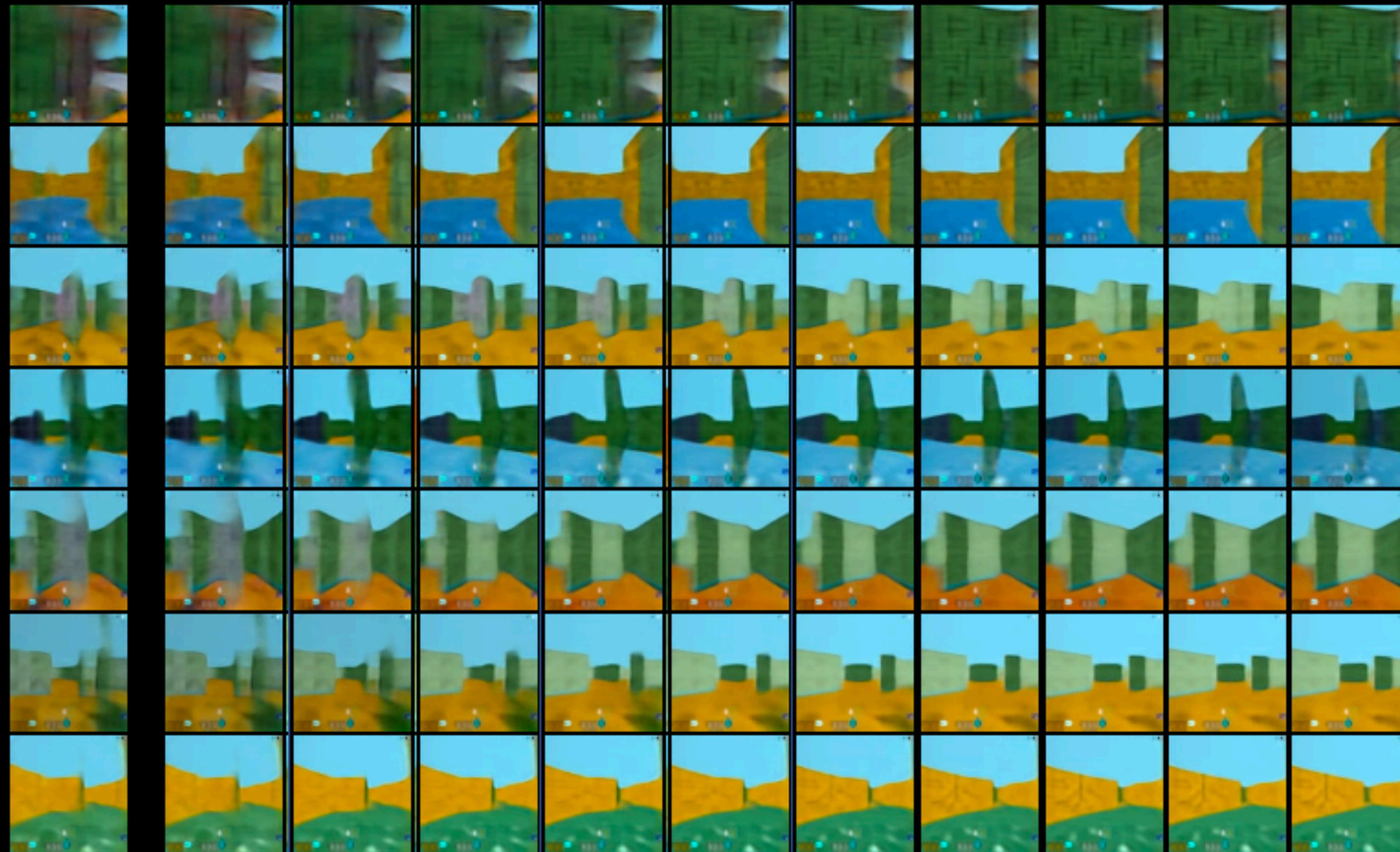
$$\ln p(X | M) \geq \mathcal{L}_T$$

	Binarized MNIST (nats/image)	Binarized Omniglot (nats/ image)	Fashion MNIST (bits/dim)	CIFAR10 (bits/dim)	DMLab mazes (bits/dim)
VMA (Bornschein, 2017)	-	103.6	-	-	-
KM (Wu, 2018a)	-	$\leq 68.3$	-	$\leq 4.37$	-
DNC (Graves, 2016)	-	$\leq 100$	-	-	-
DKM (Wu 2018b)	$\leq 75.3$	$\leq 77.2$	-	$\leq 4.79$	$\leq \textcolor{red}{2.75}$
DKM w/ TSM (our impl)	$\leq 51.84$	$\leq 70.88$	$\leq 4.15$	$\leq 4.31$	$\leq 2.92$
K++ (ours)	$\leq \textcolor{red}{41.58}$	$\leq \textcolor{red}{66.24}$	$\leq \textcolor{red}{3.4}$	$\leq \textcolor{red}{3.28}$	$\leq 2.88$



# Improving generations through iterative inference.

Initial generation



Iterative inference





# DMLab maze generation.

$$y_t \sim p(Y), \epsilon \sim \mathcal{N}(0, 0.01)$$

$$y_t \sim p(Y)$$



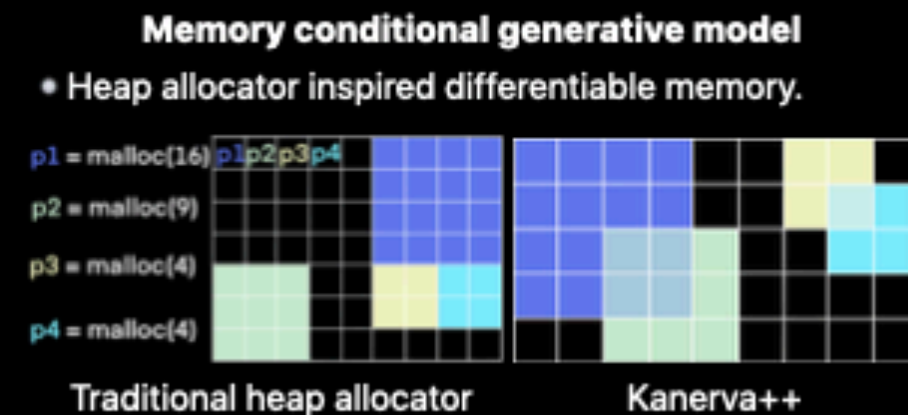


# Poster #1802

## May 6, session 10

### Kanerva++: extending the Kanerva Machine with differentiable, locally block allocated latent memory.

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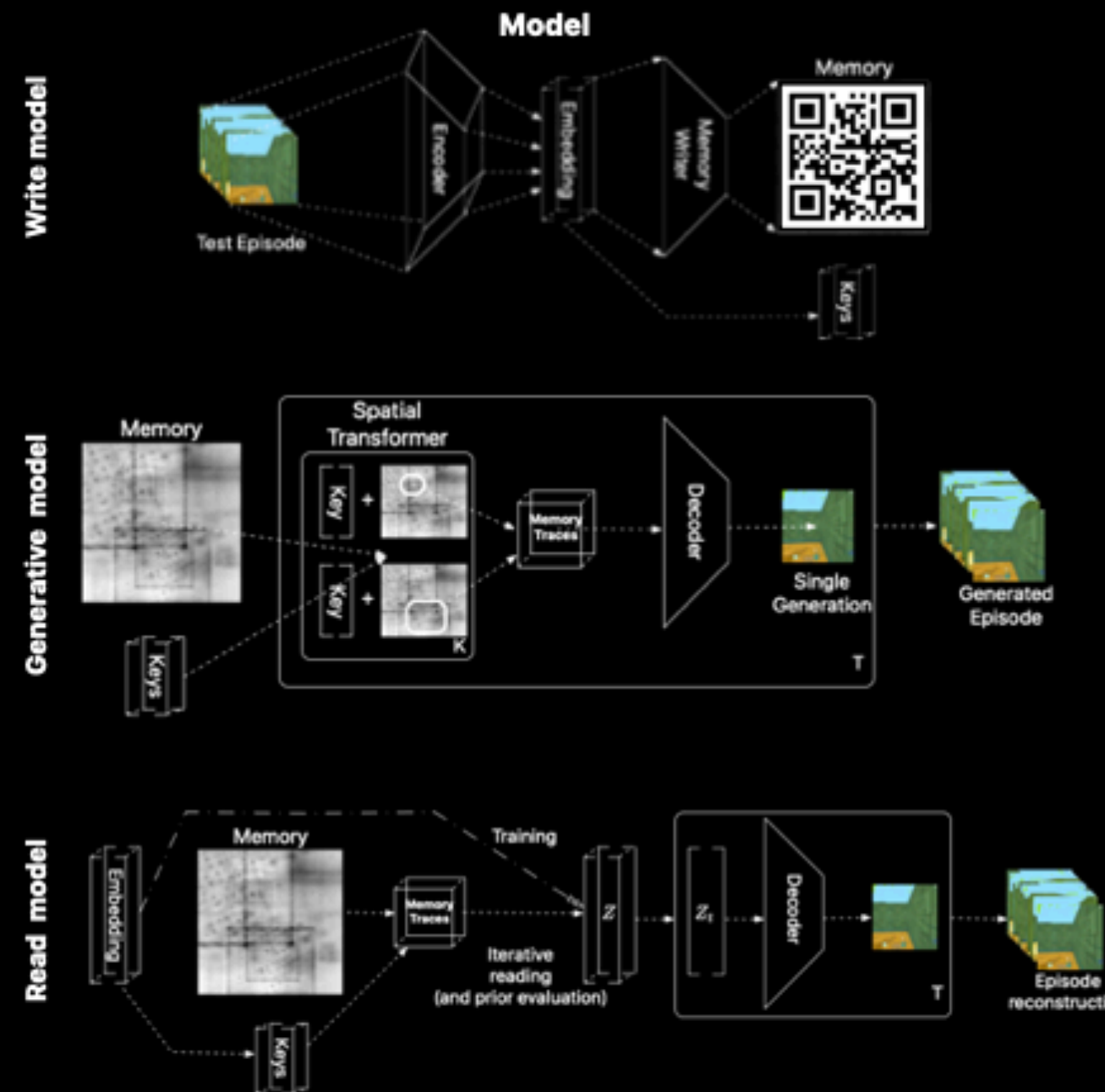
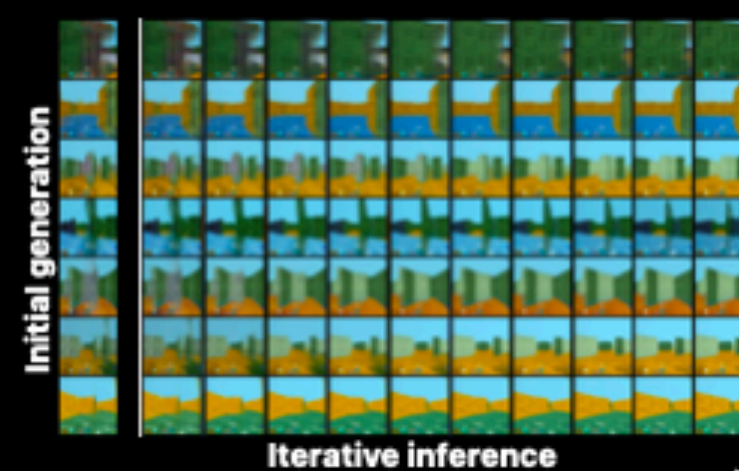


**We propose**

Kanerva++: a differentiable, **end-to-end** block allocated episodic memory for conditional image generation.

#### Contributions

- Deterministic **episodic memory** created through temporal shift module encoder.
- Spatial transformer based **block allocation**.
- **Low dimensional sampling distribution** ( $\mathbb{R}^3$ ) that indexes large memory.
- Local key perturbations produce **semantically meaningful generations**.



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K++ (ours)	≤ 41.58	≤ 66.24	≤ 3.40	≤ 3.28	≤ 2.88

